Claims

- An automated method for frequency compensated communications reception characterised in that it includes compensating for frequency offset in a received signal by adaptively forming a combination of basis functions and a training sequence that collectively approximate to a desired frequency-shifted signal to be acquired.
- 2. A method according to Claim 1 characterised in that it includes constructing a reference signal or comparison training sequence that is an adaptively formed combination of basis functions and the training sequence.
- 3. A method according to Claim 2 for acquiring a signal with a receiver having multiple antenna elements, characterised in that the method includes constructing the reference signal by minimising a cost function constructed from an adaptively weighted combination of basis functions, a training sequence and a received signal, together with a constraint to obtain non-trivial solutions.
- 4. A method according to Claim 3 characterised in that the constraint requires non-zero signal power.
- 5. A method according to Claim 3 characterised in that the cost function is J given by: $J = \|\mathbf{X}\mathbf{w} \mathbf{C}\mathbf{F}\mathbf{v}\|^2 + \lambda \left(\mathbf{w}^H\mathbf{X}^H\mathbf{X}\mathbf{w} 1\right), \text{ where } \mathbf{X} \text{ is a matrix of received signal samples, } \mathbf{w} \text{ is a vector of beamforming weights which are adaptive to minimise } J, \\ \mathbf{C} \text{ is a diagonal matrix having elements of the training sequence on its diagonal, } \mathbf{F} \\ \text{is a matrix having columns defining respective basis functions, } \mathbf{v} \text{ is a vector of weights which are adaptive to minimise } J, \text{ superscript index } H \text{ indicates a complex conjugate transpose and } \lambda \text{ is a Lagrange multiplier and the term which incorporates it is to constrain beamformer output power to be non-zero.}$
- 6. A method according to Claim 5 characterised in that it includes determining the adaptive weight vectors w and v at intervals from true estimates of a correlation matrix determined from multiple data vectors and from inverses of such estimates recursively updated to reflect successive new data vectors which are rows of the matrix X.

- 7. A method according to Claim 6 characterised in that it includes recursively updating inverse correlation matrices by:
 - forming a vector $\mathbf{u}(n)$ having a first element $\mathbf{u}_1(n)$ equal to $\sqrt{U_{1,1}(n)}$ and other elements $\mathbf{u}_p(n)$ (p= 2 to M) which are respective ratios $\mathbf{U}_{p,1}(n)/\mathbf{u}_1(n)$, $\mathbf{U}_{p,1}(n)$ is a pth element of a first column of a matrix $\mathbf{U}(n)$, the matrix $\mathbf{U}(n) \equiv \mathbf{u}(n)\mathbf{u}^H(n) = \mathbf{x}(n)\mathbf{x}^H(n) \mathbf{x}(n-K+1)\mathbf{x}^H(n-K+1)$, $\mathbf{x}(n)$ is a most recent data vector and $\mathbf{x}(n-K+1)$ is a least recent data vector involved in updating and $\mathbf{x}(n)\mathbf{x}^H(n)$ and $\mathbf{x}(n-K+1)\mathbf{x}^H(n-K+1)$ are correlation matrices;
 - b) premultiplying a previous inverse correlation matrix $\mathbf{P}(n-1)$ by vector $\mathbf{u}^H(n)$ and postmultiplied by vector $\mathbf{u}(n)$ to form a product and adding the product to a forget factor to form a sum;
 - postmultiplying the previous inverse correlation matrix P(n-1) by vector $\mathbf{u}(n)$ and dividing by the said sum to form a quotient; and
 - d) subtracting the quotient from the previous inverse correlation matrix P(n-1) to provide a difference.
- 8. A method according to Claim 2 for acquiring a signal with a receiver having a single antenna element, characterised in that the method includes constructing the reference signal by minimising a cost function constructed from an adaptively weighted combination of basis functions, a scaled received signal and a constraint requiring non-zero signal power.
- 9. A method according to Claim 8 characterised in that the cost function is J given by: $J = \|\mathbf{x} \mathbf{CFv}\|^2$, where \mathbf{x} is a vector of received signal samples, and \mathbf{v} , \mathbf{C} and \mathbf{F} are as defined earlier.
- 10. A method according to Claim 8 characterised in that the cost function is J given by: $J = \|\alpha \mathbf{x} \mathbf{G} \mathbf{v}\|^2 + \lambda \left(\alpha^* \mathbf{x}^H \mathbf{x} \alpha 1\right), \text{ where } \alpha \text{ is a scaling factor, } \mathbf{x} \text{ is a vector of received signal samples, } \mathbf{G} \text{ is a matrix equal to } \mathbf{CF} \text{ and } \mathbf{v}, \lambda, \mathbf{C}, \mathbf{F} \text{ and } H \text{ are } \mathbf{v} = 0$

as defined earlier.

- 11. Apparatus for frequency compensated communications reception characterised in that it includes means for compensating for frequency offset in a received signal by adaptively forming a combination of basis functions and a training sequence that collectively approximate to a desired frequency-shifted signal to be acquired.
- 12. Apparatus according to Claim 11 characterised in that it includes means for constructing a reference signal or comparison training sequence that is an adaptively formed combination of basis functions and the training sequence.
- 13. Apparatus according to Claim 12 having a receiver with multiple antenna elements for acquiring the received signal, characterised in that the apparatus includes means for constructing the reference signal by minimising a cost function constructed from an adaptively weighted combination of basis functions, a training sequence and a received signal, together with a constraint to obtain non-trivial solutions.
- 14. Apparatus according to Claim 13 characterised in that the constraint requires non-zero signal power.
- 15. Apparatus according to Claim 13 characterised in that the cost function is J given by: $J = \|\mathbf{X}\mathbf{w} \mathbf{CFv}\|^2 + \lambda \left(\mathbf{w}^H \mathbf{X}^H \mathbf{X}\mathbf{w} 1\right)$, where \mathbf{X} is a matrix of received signal samples, \mathbf{w} is a vector of beamforming weights which are adaptive to minimise J, C is a diagonal matrix having elements of the training sequence on its diagonal, F is a matrix having columns defining respective basis functions, \mathbf{v} is a vector of weights which are adaptive to minimise J, superscript index H indicates a complex conjugate transpose and λ is a Lagrange multiplier and the term which incorporates it is to constrain beamformer output power to be non-zero.
- 16. Apparatus according to Claim 15 characterised in that it includes means for determining the adaptive weight vectors w and v at intervals from true estimates of a correlation matrix determined from multiple data vectors and from inverses of such estimates recursively updated to reflect successive new data vectors which are rows of the matrix X.

- 17. Apparatus according to Claim 16 characterised in that it includes means for recursively updating inverse correlation matrices by:
 - forming a vector $\mathbf{u}(n)$ having a first element $\mathbf{u}_1(n)$ equal to $\sqrt{U_{1,1}(n)}$ and other elements $\mathbf{u}_p(n)$ (p= 2 to M) which are respective ratios $U_{p,1}(n)/\mathbf{u}_1(n)$, $U_{p,1}(n)$ is a pth element of a first column of a matrix $\mathbf{U}(n)$, the matrix $\mathbf{U}(n) \equiv \mathbf{u}(n)\mathbf{u}^H(n) = \mathbf{x}(n)\mathbf{x}^H(n) \mathbf{x}(n-K+1)\mathbf{x}^H(n-K+1)$, $\mathbf{x}(n)$ is a most recent data vector and $\mathbf{x}(n-K+1)$ is a least recent data vector involved in updating and $\mathbf{x}(n)\mathbf{x}^H(n)$ and $\mathbf{x}(n-K+1)\mathbf{x}^H(n-K+1)$ are correlation matrices;
 - premultiplying a previous inverse correlation matrix P(n-1) by vector $\mathbf{u}^H(n)$ and postmultiplied by vector $\mathbf{u}(n)$ to form a product and adding the product to a forget factor to form a sum;
 - c) postmultiplying the previous inverse correlation matrix P(n-1) by vector $\mathbf{u}(n)$ and dividing by the said sum to form a quotient; and
 - d) subtracting the quotient from the previous inverse correlation matrix P(n-1) to provide a difference.
- 18. Apparatus according to Claim 12 having a receiver with a single antenna element for acquiring the received signal, characterised in that the apparatus includes means for constructing the reference signal by minimising a cost function constructed from an adaptively weighted combination of basis functions, a scaled received signal and a constraint requiring non-zero signal power.
- Apparatus according to Claim 18 characterised in that the cost function is J given by: $J = \|\mathbf{x} \mathbf{CFv}\|^2$, where \mathbf{x} is a vector of received signal samples, and \mathbf{v} , \mathbf{C} and \mathbf{F} are as defined earlier.
- 20. Apparatus according to Claim 18 characterised in that the cost function is J given by: $J = \|\alpha \mathbf{x} \mathbf{G} \mathbf{v}\|^2 + \lambda \left(\alpha^* \mathbf{x}^H \mathbf{x} \alpha 1\right)$, where α is a scaling factor, \mathbf{x} is a vector of received signal samples, \mathbf{G} is a matrix equal to \mathbf{CF} and \mathbf{v} , λ , \mathbf{C} , \mathbf{F} and H are

as defined earlier.

- 21. Computer software for controlling a computer processor and for use in frequency compensated communications reception characterised in that it includes program code instructions for compensating for frequency offset in a received signal by adaptively forming a combination of basis functions and a training sequence that collectively approximate to a desired frequency-shifted signal to be acquired.
- 22. Computer software according to Claim 21 characterised in that it includes program code instructions for constructing a reference signal or comparison training sequence that is an adaptively formed combination of basis functions and the training sequence.
- 23. Computer software according to Claim 22 for use in processing received signals acquired by a receiver with multiple antenna elements, characterised in that the computer software includes program code instructions for constructing the reference signal by minimising a cost function constructed from an adaptively weighted combination of basis functions, a training sequence and a received signal, together with a constraint to obtain non-trivial solutions.
- 24. Computer software according to Claim 23 characterised in that the constraint requires non-zero signal power.
- Computer software according to Claim 23 characterised in that the cost function is J given by: $J = \|\mathbf{X}\mathbf{w} \mathbf{CFv}\|^2 + \lambda \left(\mathbf{w}^H \mathbf{X}^H \mathbf{X} \mathbf{w} 1\right)$, where \mathbf{X} is a matrix of received signal samples, \mathbf{w} is a vector of beamforming weights which are adaptive to minimise J, C is a diagonal matrix having elements of the training sequence on its diagonal, \mathbf{F} is a matrix having columns defining respective basis functions, \mathbf{v} is a vector of weights which are adaptive to minimise J, superscript index H indicates a complex conjugate transpose and λ is a Lagrange multiplier and the term which incorporates it is to constrain beamformer output power to be non-zero.
- 26. Computer software according to Claim 25 characterised in that it includes program code instructions for determining the adaptive weight vectors w and v at intervals from true estimates of a correlation matrix determined from multiple data vectors

and from inverses of such estimates recursively updated to reflect successive new data vectors which are rows of the matrix \mathbf{X} .

- 27. Computer software according to Claim 26 characterised in that it includes program code instructions for recursively updating inverse correlation matrices by:
 - forming a vector $\mathbf{u}(n)$ having a first element $\mathbf{u}_1(n)$ equal to $\sqrt{U_{1,1}(n)}$ and other elements $\mathbf{u}_p(n)$ (p= 2 to M) which are respective ratios $\mathbf{U}_{p,1}(n)/\mathbf{u}_1(n)$, $\mathbf{U}_{p,1}(n)$ is a pth element of a first column of a matrix $\mathbf{U}(n)$, the matrix $\mathbf{U}(n) \equiv \mathbf{u}(n)\mathbf{u}^H(n) = \mathbf{x}(n)\mathbf{x}^H(n) \mathbf{x}(n-K+1)\mathbf{x}^H(n-K+1)$, $\mathbf{x}(n)$ is a most recent data vector and $\mathbf{x}(n-K+1)$ is a least recent data vector involved in updating and $\mathbf{x}(n)\mathbf{x}^H(n)$ and $\mathbf{x}(n-K+1)\mathbf{x}^H(n-K+1)$ are correlation matrices;
 - premultiplying a previous inverse correlation matrix $\mathbf{P}(n-1)$ by vector $\mathbf{u}^H(n)$ and postmultiplied by vector $\mathbf{u}(n)$ to form a product and adding the product to a forget factor to form a sum;
 - c) postmultiplying the previous inverse correlation matrix P(n-1) by vector $\mathbf{u}(n)$ and dividing by the said sum to form a quotient; and
 - d) subtracting the quotient from the previous inverse correlation matrix P(n-1) to provide a difference.
- 28. Computer software according to Claim 22 for use in processing received signals acquired by a receiver with a single antenna element, characterised in that the computer software includes program code instructions for constructing the reference signal by minimising a cost function constructed from an adaptively weighted combination of basis functions, a scaled received signal and a constraint requiring non-zero signal power.
- Computer software according to Claim 28 characterised in that the cost function is J given by: $J = \|\mathbf{x} \mathbf{CFv}\|^2$, where \mathbf{x} is a vector of received signal samples, and \mathbf{v} , \mathbf{C} and \mathbf{F} are as defined earlier.

Computer software according to Claim 28 characterised in that the cost function is J given by: $J = \|\alpha \mathbf{x} - \mathbf{G} \mathbf{v}\|^2 + \lambda \left(\alpha^* \mathbf{x}^H \mathbf{x} \alpha - 1\right)$, where α is a scaling factor, \mathbf{x} is a vector of received signal samples, \mathbf{G} is a matrix equal to \mathbf{CF} and \mathbf{v} , λ , \mathbf{C} , \mathbf{F} and \mathbf{H} are as defined earlier.